

Multilayer Perceptron based Recommender System

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Introduction: MLP

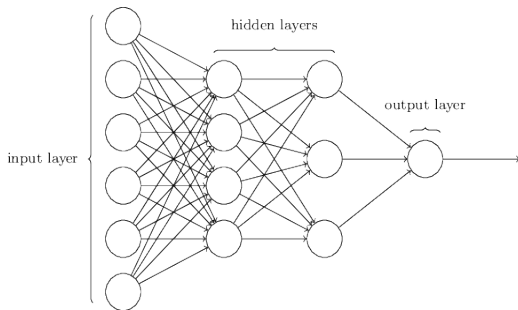


Figure: Multilayer Perceptron

Introduction: MLP

- Concise but effective model.
- Widely used in many area
- Approximate any measurable function to any desired degree of accuracy.

Introduction : Recommender System

Recommendation models are mainly categorized into...

- Collaborative Filtering Recommender System
 - By learning from user - item historical interactions
- Content-based Recommender System
 - Using item's and user's auxiliary information.
- Hybrid Recommender System

Capture the **non-linear relationships** between users and item by MLP

Neural Collaborative Filtering

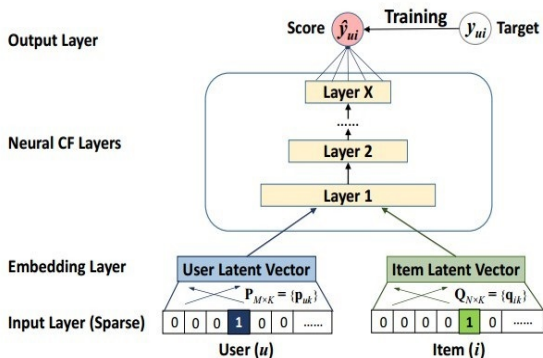


Figure: Neural Collaborative Filtering

Neural Collaborative Filtering

- $Y = \{y_{ui}\}_{(u=1,\dots,M,i=1,\dots,N)}$, ($R = \{r_{ui}\}_{(u=1,\dots,M,i=1,\dots,N)}$)
 , User-Item Rating Matrix
- s_u^{user} , One-hot identifier of user u , ($u=1,\dots,M$)
- s_i^{item} , One-hot identifier of item i , ($i=1,\dots,N$)
- $P \in R^{M \times K}$, $Q \in R^{N \times K}$
 , the latent factor matrix for users and items, respectively

Learning from implicit feedback

- User-Item interaction : explicit feedback vs [implicit feedback](#)
- Define interaction(rating) matrix $Y = \{y_{ui}\}_{(u=1,\dots,M,i=1,\dots,N)}$

$$y_{ui} = \begin{cases} 1, & \text{if interaction (user } u, \text{ item } i) \text{ is observed;} \\ 0, & \text{otherwise.} \end{cases}$$

- Implicit data provides only noisy signals
- Scarcity of negative feedback
- The problem of estimating the scores of unobserved entries Y

Matrix Factorization

- Predict rating matrix by introducing the latent vector for user and item.
- Let $p_u = P^T s_u^{user} \in R^K$, and $q_i = Q^T s_i^{item} \in R^K$ denote the latent vector for user u and item i
- MF estimates an interaction y_{ui} as the inner product of u_u , and v_i

$$\hat{y}_{ui} = f(u, i | p_u, q_i) = p_u^T q_i$$

- Matrix Factorization have limitations

Neural Collaborative Filtering

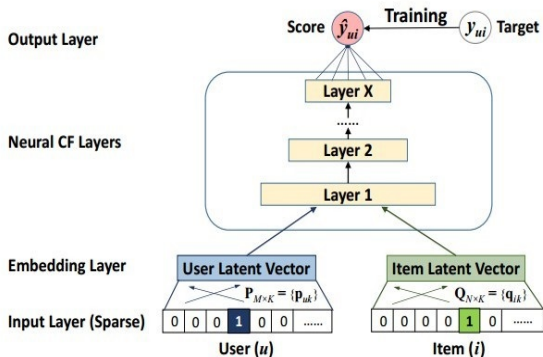


Figure: Neural Collaborative Filtering

Neural Collaborative Filtering

- The prediction rule of NCF is formulated as follows:

$$\hat{y}_{ui} = f(U^T \cdot s_u^{user}, V^T \cdot s_i^{item} | U, V, \theta)$$

$f(\cdot)$: multilayer perceptron, θ : parameters of this network.

- The (general) loss function is

$$L = \sum_{(u,i) \in O \cup O^-} w_{ui} (y_{ui} - \hat{y}_{ui})^2$$

O : observed interaction,

O^- : all(or sampled from) unobserved interactions

w_{ui} : weight(a hyperparameter)

Neural Collaborative Filtering

- For implicit feedback, Use Logistic or Probit function
- The loss function is

$$L = \sum_{(u,i) \in O \cup O^-} y_{ui} \log \hat{y}_{ui} + (1 - y_{ui}) \log(1 - \hat{y}_{ui})$$

O : observed interaction,

O^- : all(or sampled from) unobserved interactions

- O^- : uniformly sample them from unobserved interactions.
- Minimize L by Stochastic gradient descent(SGD)

Fusion of GMF and NCF

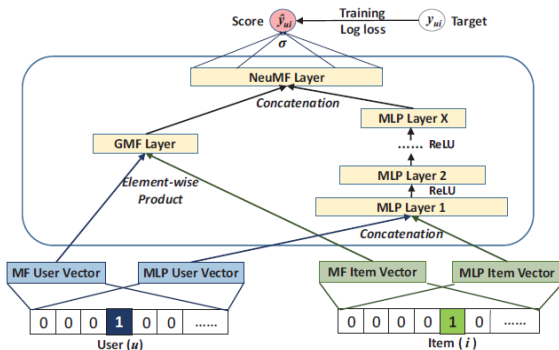


Figure: Neural matrix factorization model

- Generalized Matrix Factorization(GMF):

$$\hat{y}_{GMF} = f_{out}(w^T(\hat{y}_{MF})) = f_{out}(w^T(p_u^T q_i))$$

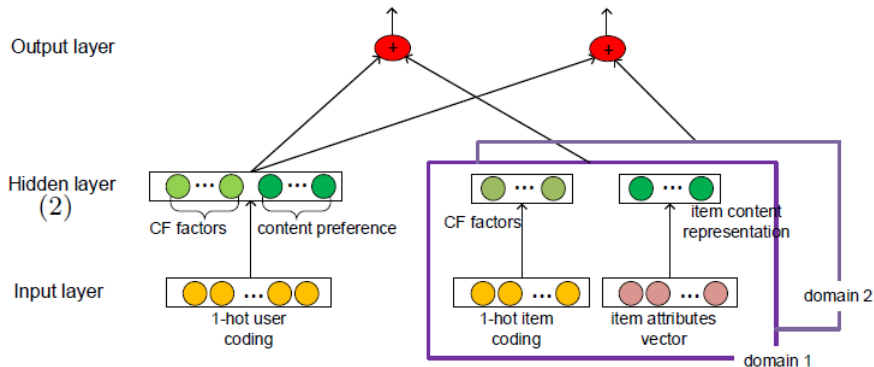


Figure: CCCFNet

- Cross-domain Content-boosted Collaborative Filtering neural Network.
- Combine collaborative filtering and content filtering.
- Introduce multiple-domain, use knowledge from relatively dense auxiliary domains to overcome sparsity problem.
- Consistently, outperforms several baseline method.

- Suppose we have two domains: Target (1) & Auxiliary(2)
- $Y_{N \times M^{(1)}}^{(1)}, Y_{N \times M^{(2)}}^{(2)}$, Rating matrix
- $A_{M^{(1)} \times T^{(1)}}^{(1)}, A_{M^{(2)} \times T^{(2)}}^{(2)}$, Content matrix (with $T^{(1)}, T^{(2)}$ attribute)
- $P_{N \times K}, Q^{(1)}_{M^{(1)} \times K}, Q^{(2)}_{M^{(2)} \times K}$, Latent factor matrix for users and items
- $U_{N \times L}, V^{(1)}_{T^{(1)} \times L}, V^{(2)}_{T^{(2)} \times L}$, Latent factor matrix for content preference, item content
- $\theta = (P, U, Q^{(1)}, Q^{(2)}, V^{(1)}, V^{(2)})$

- Minimize the following equation:

$$L = \frac{1}{2} \sum_{u,i} (y_{ui}^{(1)} - p_u \cdot q_i^{(1)} - u_u \cdot v_i^{(1)})^2 + \frac{\lambda_1}{2} \sum_{u,i} (y_{ui}^{(2)} - p_u \cdot q_i^{(2)} - u_u \cdot v_i^{(2)})^2 + \frac{\lambda_*}{2} \sum_k (\|\theta\|)^2$$

- $p_u = P^T s_u^{user}$, $q_i = Q^T s_u^{item}$, $u_u = U^T s_u^{user}$, $v_i = \text{row}(A, i) V^T$

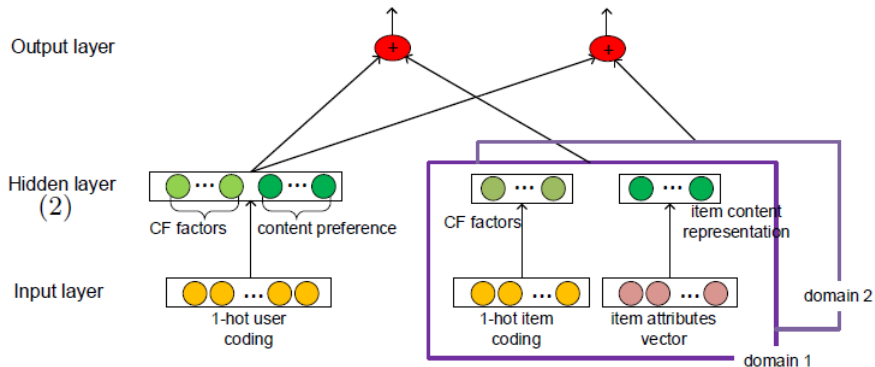


Figure: CCCFNet

Wide & Deep Learning

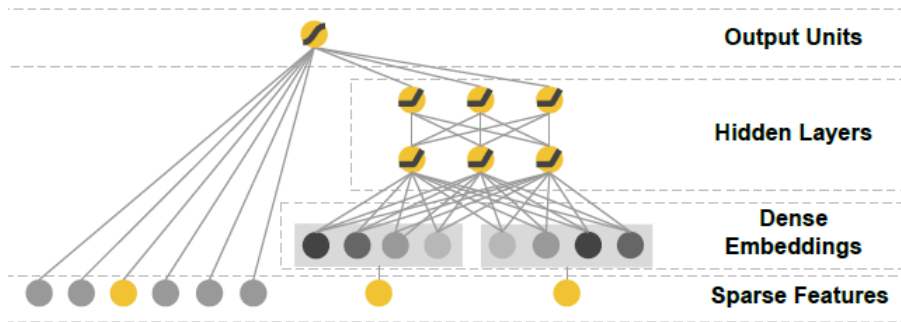


Figure: Wide & Deep Learning

- Wide Learning Components

- Single layer Perceptron
- Memorization
 - Catching the direct features from historical data
 - Loosely defined: Learning the frequent co-occurrence of items or features, and exploiting the correlation in the historical data

- Deep Learning Components

- Multilayer Perceptron
- Generalization
 - Catching the generalized by producing more general and abstract representations
 - Loosely defined: Learning the transitivity of correlation and explores new feature combinations that have never or rarely occurred in the past.

- The wide learning part

$$y = W_{wide}^T(x, \phi(x)) + b$$

- $\phi(x)$ is cross-product transformation which is defined as:

$$\phi_k(x) = \prod_{i=1}^d x_i^{c_{ki}}, c_{ki} \in \{0, 1\}$$

$$c_{ki} = \begin{cases} 1, & \text{if } i\text{-th feature is part of the } k\text{-th transformation } \phi(x) \\ 0, & \text{otherwise.} \end{cases}$$

- Cross-product transformation is manually designed

- The deep learning part

$$\alpha^{(l+1)} = f(W_{deep}^{(l)}\alpha^{(l)} + b)$$

- The wide & deep learning model is attained by fusing these two models:

$$P(\hat{y}_{ui} = 1 | x) = \sigma(W_{wide}^T \{x, \phi(x)\} + W_{deep}^{(T)}\alpha^{(ITf)} + bias)$$

Wide & Deep Learning

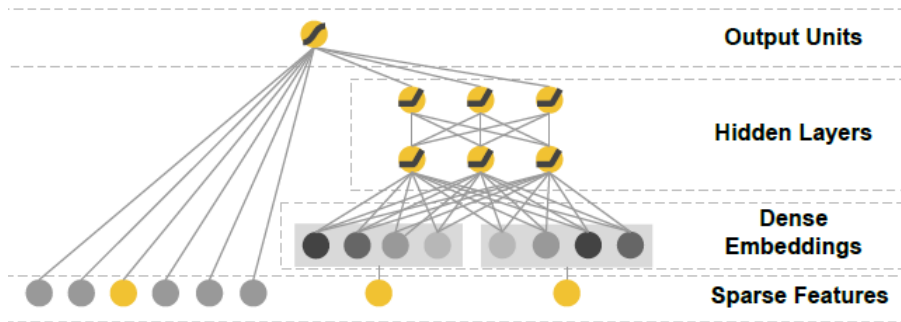


Figure: Wide & Deep Learning

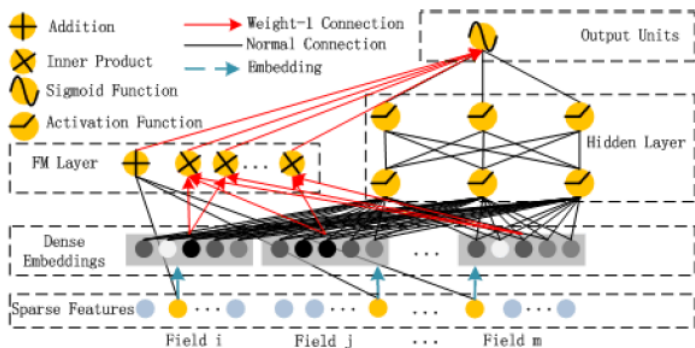


Figure: DeepFM

- Deep Factorization Machine
- Enlightend by Wide & Deep Learning
- Integrates Factorization Machine and MLP
- Capture the high-order feature interactions via deep neural network.
- Capture the low-order feature interactions via factorization machine.
- Does not require tedious feature engineering.

- x is an m -fields data consisting of pairs (u, i) , and d -dimensional vector
- x may include categorical fields (gender, location...) and continuous fields (age...)
- $x = [x_{field_1}, x_{field_2}, \dots, x_{field_m}]$ is d -dimensional vector.
- $\hat{y} = \sigma(y_{FM}(x), y_{MLP}(x))$
- FM component and Deep component, that share the same input.

FM Component

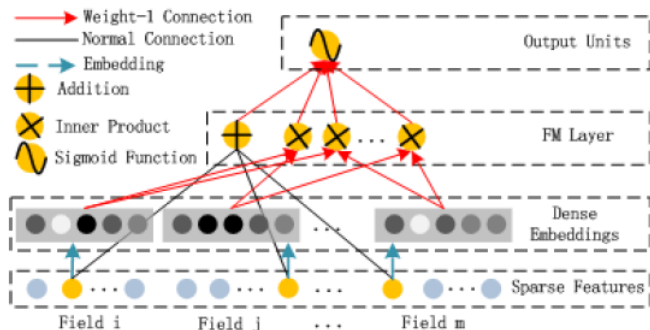


Figure: FM Component

- It can capture order-2 feature interactions much more effectively than previous approach.(especially the dataset is sparse)

$$\hat{y}_{FM} = \langle w, x \rangle + \sum_{i=1}^m \sum_{j=i+1}^m \langle V_i, V_j \rangle x_i \cdot x_j$$

, $w \in R^d$ and $V_i \in R^k$

- $\langle w, x \rangle$ reflects order-1 feature interactions, and summation term reflects order-2 feature interactions.

Deep Component

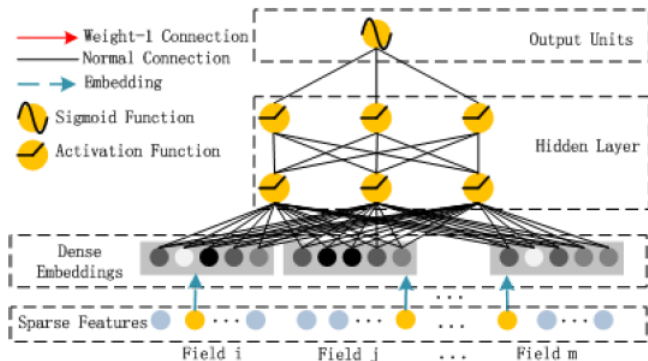


Figure: Deep Component

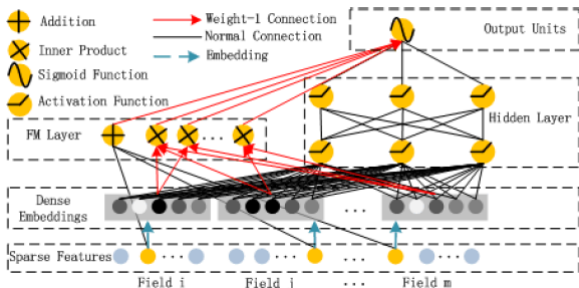


Figure: DeepFM

$$\hat{y} = \sigma(\langle w, x \rangle + \sum_{i=1}^m \sum_{j=i+1}^m \langle V_i, V_j \rangle x_i \cdot x_j + W_{deep}^{(T)} \alpha^{(l_f)} + bias)$$

The End