

CTR prediction models

Choi.Y

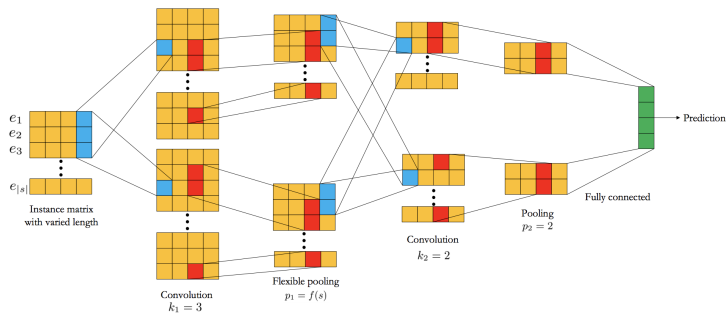
2018.06.28

A Convolutional Click Prediction Model

Click prediction

- Assume that there are historical click sequences.
- RNN is a good model for sequential data.
- Historical click sequence of a certain user is divided by different time intervals.
- RNN may have its limitation for these.
- CNN architecture can fully extract local-global key feature.

Structure



Notation

- $e_j \in R^d$ where e_j is an embedding vector
- $w \in R^d$ is a weight matrix
- $s = [e_1, \dots, e_n] \in R^{d \times n}$ is a instance matrix.

Convolution layer

- One-dimensional Convolution step.
- Given w_i, s_i , convolution output $r_i = w_i^T s_{i,j-\omega+1:j}$
for $j = 1, \dots, n + \omega - w$
- The optimized weight in the filter w detects feature and recognizes specific ranges of neighborhood in input instance.

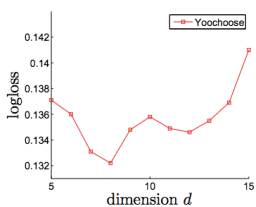
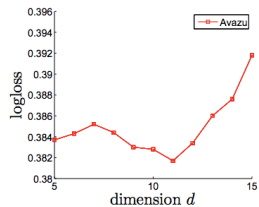
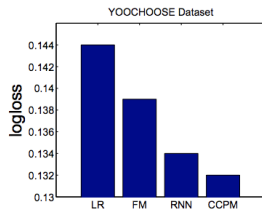
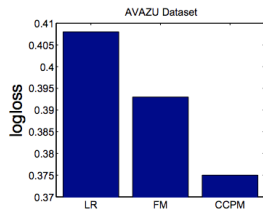
Flexible p-max pooling layer

- Given a convolutional output vector $r_i \in R^n$
- p-max pooling selects a sub-vector $s_i \in R^p$ which contains the p biggest values in r_i
- This strategy is due to the difference of each user's instance dimension.
- $$p_i = \begin{cases} (1 - (i/l)^{l-i})n & i = 1, \dots, l - 1 \\ 3 & i = l \end{cases}$$
- where l is the total number of convolutional layers, n is the length of the input instance.

Feature Maps

- Use $\tanh(x) = \frac{\exp(x) - \exp(-x)}{\exp(x) + \exp(-x)}$
- F^i : i-th order feature map (convolution + pooling + activation)
- $F_j^i = \sum_{k=1}^{m_i} w_{j,k}^i * F_k^{i-1}$
- softmax + negative log likelihood

Result



Position-Normalized Click prediction in Search Advertising

Biased CTR estimates

- The observed click-through data has been confounded by positional bias.
- Since users tend to click more on ads shown in higher position.
- Want to find position-denoised CTR

Notation

- i : a query-ad pair
- j : ad position
- v : the number of ad impressions.
- The observed CTR = $p(\text{click}|i, j)$

Assumption

1. Clicking an ad is independent of its position, given that it is physically examined.
2. Examining an ad is independent of its content or relevance, given its position.
 - $p(\text{click}|i, j) = p(\text{click}|\text{exam}, i)p(\text{exam}|j)$
 - $p(\text{click}|\text{exam}, i)$, denoted as p_i , is a position-normalized CTR.
 - $p(\text{exam}|j)$, denoted as q_j , reflects the positional bias.

The binomial model

- model : $c_{ij} \sim B(v_{ij}, p_i q_j), \forall i, j$
- Training dataset $D = \{(c_{ij}, v_{ij})\}$
- parameter $\theta = (p, q)$
- $\ell(\theta) = \sum_{i,j} \log \binom{v_{ij}}{c_{ij}} c_{ij} \log(p_i q_j) + (v_{ij} - c_{ij}) \log(1 - p_i q_j)$

The binomial model

- regarding one of model parameters as latent variable(e.g. q)
- To estimate the MLE of both $\theta = (p, q)$, Use E-M Algorithm

- E-step: $q'_j \leftarrow \frac{\sum_i c_{ij}}{\sum_i (v_{ij} - c_{ij}) p_i / (1 - p_i q_j)}$

- M-step : $p'_i \leftarrow \frac{\sum_j c_{ij}}{\sum_j (v_{ij} - c_{ij}) q_j / (1 - p_i q_j)}$

The Poisson Model

- If n is sufficiently large and p is sufficiently small ($np \rightarrow \lambda$)
- We can approximate Binomial dist as Poisson dist
- Model : $c_{ij} \sim \text{Poisson}(v_{ij}p_iq_j), \forall i, j.$
- E-step: $q'_j \leftarrow \frac{\sum_i c_{ij}}{\sum_i (v_{ij}p_i)}$
- M-step : $p'_i \leftarrow \frac{\sum_j c_{ij}}{\sum_j v_{ij}q_j}$

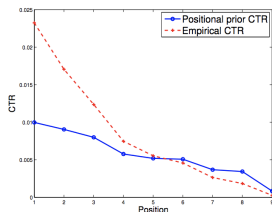
The Gamma-Poisson Model

- Impose a gamma prior on q
- $q_j \sim \text{Gamma}(\alpha, \beta), \forall j$.
- $p(D, q | p, \alpha, \beta) = \prod_{i,j} \frac{(v_{ij} p_i q_j)^{c_{ij}} \exp(-v_{ij} p_i q_j)}{c_{ij}!} \times \prod_j \frac{q_j^{\alpha-1} \exp(-q_j/\beta)}{\beta^\alpha \Gamma(\alpha)}$
- E-step: $q'_j \leftarrow \frac{\sum_i c_{ij} + (\alpha - 1)}{\sum_i (v_{ij} p_i + 1/\beta)}$
- M-step : $p'_i \leftarrow \frac{\sum_j c_{ij}}{\sum_j v_{ij} q_j}$

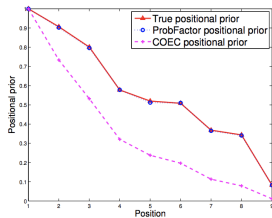
Simulation

1. \forall position $j \in [1, \dots, m]$, generate a $q_j \sim \text{Gamma}(\alpha, \beta)$; sort q in descending order, and scale q by $1/q_1$;
2. \forall query-ad pair $i \in [1, \dots, n]$, generate a $p_i \sim \text{Beta}(\gamma, \delta)$;
3. $\forall i$, generate a number of impressions $s_i \sim \text{Poisson}(\lambda)$;
4. $\forall i$, construct a multinomial distribution over positions $\phi_i \propto 1 / (p_i / \mu(p_i))^{j-1}$, to push good ads higher up;
5. $\forall i$, generate an impression allocation vector over positions $v_i \sim \text{Multinomial}(s_i, \phi_i)$, to form an $n \times m$ matrix of impression V ;
6. Derive an $n \times m$ matrix of CTRs $Z = pq^\top$;
7. Derive an $n \times m$ matrix of Poisson means $Y = V \cdot Z$, where \cdot is element-wise multiplication;
8. Generate an $n \times m$ matrix of clicks $C \sim \text{Poisson}(Y)$, and $C \leftarrow \min(C, V)$, element-wise.

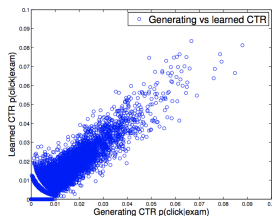
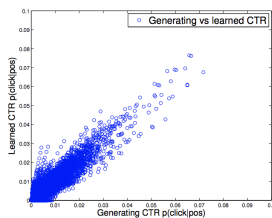
Simulation



(a) Positional prior and empirical CTR



(b) True positional, Factor and COEC learned

(a) True vs. learned $p_i = p(\text{click}|\text{exam})$ (b) True vs. learned $p_{ij} = p(\text{click}|\text{pos})$